

### Mastering Physics - Intro to Momentum (page 1)

1. Isolated systems = Momentum ( $p = m \cdot v$ ) remains constant

$$m_A v_{Ai} + m_B v_{Bi} = m_A v_{Af} + m_B v_{Bf}$$

2. a) Ball drops with the same velocity as the clay

Velocity is  $-28.4 \text{ m/s}$  at  $t = 2.9 \text{ s}$ ,  $0 \text{ m/s}$  at  $3.0 \text{ s}$ , and  $28.4 \text{ m/s}$  at  $3.1 \text{ s}$

Velocity is  $0 \text{ m/s}$  at  $t = 6.0 \text{ s} \rightarrow \text{max height}$

- b) Change in momentum of the superball is greater

- c) Impulse delivered to the superball is greater

- d) Force is greater  $J = \text{Force} \cdot \text{Time}$

3. a)  $v_f^2 = v_i^2 + 2a\Delta x \quad v_p^2 = 2(-9.8)(2) \Rightarrow v_p = -6.26 \text{ m/s}$

$$J = mv_f - mv_i = (0.1)(0) - (0.1)(-6.26) = 0.626$$

$$J = \text{Force} \cdot \Delta t$$

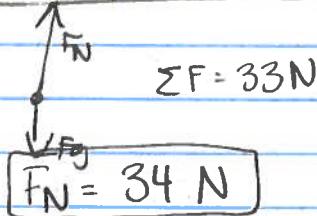
$$\Delta x = \left( \frac{v_i + v_f}{2} \right) \Delta t \quad 0.060 = \left( \frac{-6.26}{2} \right) \Delta t \quad \Delta t = 0.019 \text{ s}$$

$$0.626 = \text{Force} \cdot 0.019 \quad \boxed{\text{Force} = 33 \text{ N} \rightarrow \text{likely to bruise}}$$

b)  $a = \frac{v_f - v_i}{\Delta t} = \frac{6.26}{0.09} = 32.6 \text{ m/s}^2$

$$F = m \cdot a = 0.1 \cdot 32.6 = 33 \text{ N}$$

$$\Sigma F = F_N - F_g \quad 33 \text{ N} = F_N - (0.1)(9.8)$$



$$F_N = 34 \text{ N}$$

4. a)  $J = F \cdot t = (12000)(0.0007) = 8.4 \text{ N} \cdot \text{s}$

b) Area of the rectangle = impulse

c) Graphs have area in common

d) Negative impulse

e)  $-8.4 = (0.145)(32) + (0.145)v_f \quad v_f =$

5. a)  $p = m \cdot v$  so find this for each car

b) Impulse needed to stop them =  $\Delta \text{momentum}$  (same ranking)

c) Can't determine the force needed because we don't know the braking times

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16. a) Initial momentum = 0 (not moving)  
 b) Equal to = third law pairs      c) -500 kg·m/s (conservation of momentum)

17. a)  $J = P_f - P_i$        $J = (80)(16) - 0 = 1280$

$J = \text{Force} \cdot \text{Time}$        $1280 = 16,000 \cdot \text{Time}$

$$t = 0.08 \text{ s}$$

b)  $V_i = 16 \frac{\text{m}}{\text{s}}$        $V_f = 0 \frac{\text{m}}{\text{s}}$        $\Delta t = 0.08 \text{ s}$        $\Delta x = ?$

$$\Delta x = \left( \frac{V_i + V_f}{2} \right) \Delta t = \left( \frac{16}{2} \right) (0.08)$$

$$\Delta x = 0.64 \text{ m}$$

18. Equal masses  $\rightarrow$  Final velocity is halfway between initial velocities

19. Speed of the wagon doesn't change (no external force)

20. Momentum is constant and force of air on balloon = balloon on air

21.  $P_A > P_B$  because A takes a longer time so the force is exerted over a longer period

22. A finger exerts a smaller force but over a longer time interval

23. Momentum is constant in an isolated system

24. Freely falling metal ball when the ball is the system has increasing momentum

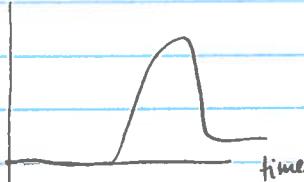
25. Retractable bumper because it increases the time of impact

26. Tennis ball hits the racket and travels in the other direction

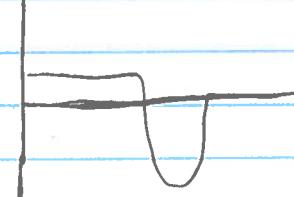
27. Greatest change in speed when the ball bounces off in the other direction

28. a)

Force



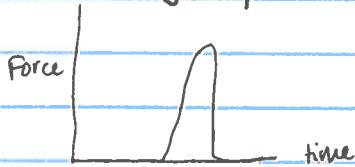
- b)



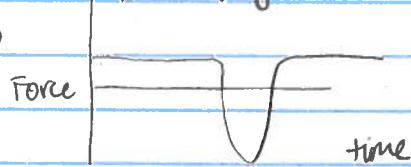
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~~19.~~ a)



b)



~~20.~~ Momentum is proportional to the mass, momentum in an isolated system is conserved, momentum is a vector, change in momentum is impulse, change in momentum is proportional to the external force

~~21.~~ Woodpeckers smack their beaks (not head) against the trees

~~22.~~ Closed, decrease, total momentum of the closed system, external



~~24.~~ Positive, negative, zero

~~25.~~ A ball that rebounds off the wall has a greater  $\Delta p$

~~26.~~ Wall exerts a greater force on the ball that bounces off

~~27.~~ an isolated, Newton's laws

~~28.~~ a) Bar has 0 horizontal velocity with respect to the truck or with respect to the Earth  $\rightarrow$  two answers

b)



c) Horizontal momentum of the whole system doesn't change, but that consists of the truck and the bar now, so the momentum of the truck decreases

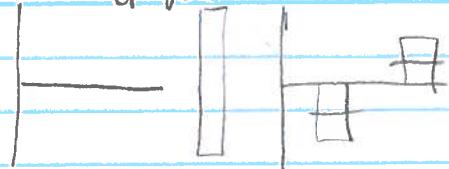
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B29. a)

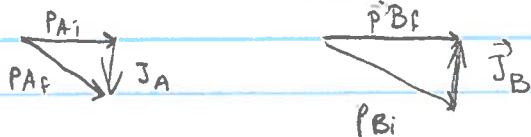


b)



B30. a)  $2p_i = p_f$  Direction changes going into and out of the incline

b)



B31. Same momentum  $p = m \cdot v$

$$B32. (m)(\frac{1}{2}v) + (m)(v) = (m)(0.75v)$$

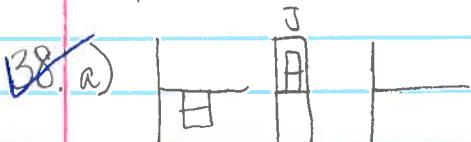
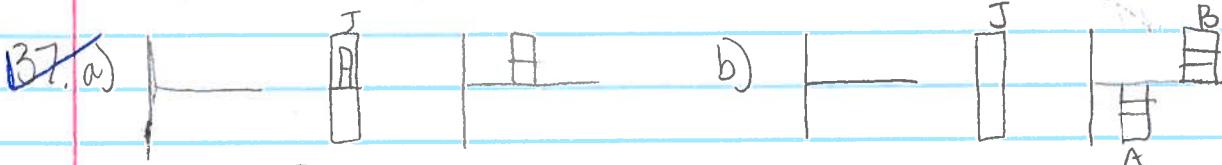
B33. Impulse = Area under Force vs. time

B34. Total momentum of an isolated system is constant, vector sum of forces acting on a particle equals the rate of change of momentum of the particle with respect to time, total momentum is the vector sum

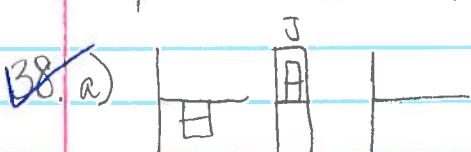
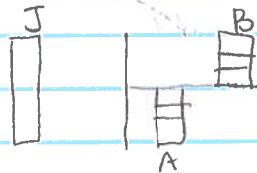
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B35. Impulse is the same (same change in velocity)

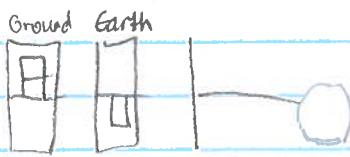
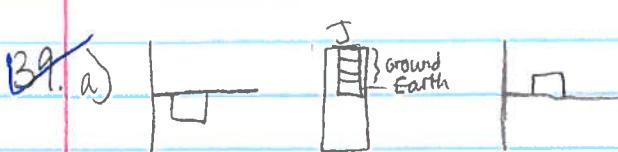
B36. Ball experiences a greater change.



b)



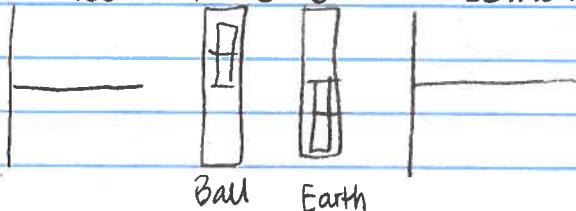
$$b) J_{N\text{on } B} = mv$$



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~~40. b) Cart won't move (no horizontal impulse)~~

b)



~~41.~~  $a = \frac{V_{\text{gas}}}{m} \cdot \frac{\Delta m}{\Delta t}$        $\Delta m = m/160$   
 $\Delta t = 1$

$a = \frac{V_{\text{gas}}}{m} \cdot \frac{m}{160} \Rightarrow V_{\text{gas}} = \frac{160}{160} \text{ m/s}$        $V_{\text{gas}} = 2560 \text{ m/s}$   
 $= 2.56 \text{ km/s}$

~~42. a)~~
 $m_{\text{Ball}} v_{\text{Ball}} = (m_{\text{Ball}} + m_{\text{olaf}}) v_{\text{Ball/olaf}}$   
 $(0.400)(10.5) = (69 + 0.4) v_{\text{Ball/olaf}}$ 
 $v_{\text{Ball/olaf}} = 0.061 \frac{\text{m}}{\text{s}}$

~~b)~~

$m_{\text{Ball}} v_{\text{Ball}} = m_{\text{Ball}} v_{\text{Ball}} + m_{\text{olaf}} v_{\text{olaf}}$   
 $(0.4)(10.5) = (0.4)(-8.1) + (69) v_{\text{olaf}}$   
 $v_{\text{olaf}} = 0.108 \frac{\text{m}}{\text{s}}$

~~43. a)~~  $p = mv = (0.057)(36) = 2.1 \text{ kg m/s}$

~~b)~~  $p = mv \quad 2.1 = 0.32 v \quad v = 6.4 \frac{\text{m}}{\text{s}}$

~~c)~~
 $M_{\text{you}} v_{\text{you}} - m_{\text{Ball}} v_{\text{Ball}}$   
 $(60)(4) - (0.057)(36) = 237.9 \text{ kg m/s}$

~~44.~~  $m = 95 \text{ g} = 0.095 \text{ kg}$        $v_i = 0 \frac{\text{m}}{\text{s}}$        $v_f = 1.2 \frac{\text{m}}{\text{s}}$

$p_i = (0.095)(0) = 0$        $p_f = (0.095)(1.2) = 0.114 \text{ kg m/s}$   
 $J = 0.114 \text{ kg m/s}$

$J = F \cdot \Delta t \quad t = 0.14 \text{ s}$

$0.114 = F \cdot 0.14$

$F = 0.814 \text{ N}$

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45.  $m = 63 \text{ kg}$   $v_i = -30 \frac{\text{m}}{\text{s}}$   $v_f = 0 \frac{\text{m}}{\text{s}}$   
 $p_i = (63)(-30) = -1890$   $p_f = 0$   $J = -1890$   
 $J = \text{Force} \cdot \Delta t$   $\Delta x = 0.50 \text{ m}$   
 $\Delta x = \left( \frac{v_i + v_f}{2} \right) \Delta t$   $0.5 = \left( \frac{-30}{2} \right) \Delta t$   $\Delta t = 0.0333$   
 $1890 = \text{Force} \cdot 0.0333$   
 $(F = 56700 \text{ N})$

46.  $v_i = -20 \frac{\text{m}}{\text{s}}$   $v_f = 0 \frac{\text{m}}{\text{s}}$   $m = 55 \text{ kg}$   $F = 8000 \text{ N}$   $\Delta x = ?$   
 $p_i = (55)(-20) = -1100 \frac{\text{kg m}}{\text{s}}$   $p_f = 0$   $J = 1100 \frac{\text{kg m}}{\text{s}}$   
 $J = F \cdot \Delta t$   $1100 = 8000 \cdot \Delta t$   $\Delta t = 0.1375 \text{ s}$   
 $\Delta x = \left( \frac{v_i + v_f}{2} \right) \Delta t$   
 $\Delta x = \left( \frac{-20}{2} \right) (0.1375)$   $\boxed{\Delta x = 1.375 \text{ m}}$