Name: _	Kathleen	Boyce

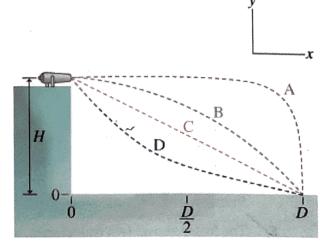
Mastering Physics 2.1 - Projectile Motion

- A cannon is fired from the top of a cliff as shown in the figure. Ignore drag (air friction) for this question. Take *H* as the height of the cliff.
  - Which of the paths would the cannonball most likely follow if the cannon barrel is horizontal?



o D

Now the cannon is pointed straight up and fired. (This procedure is not recommended!) Under the conditions already stated (drag is to be ignored) which of the following correctly describes the acceleration of the ball?



- A steadily increasing downward acceleration from the moment the cannonball leaves the cannon barrel until it reaches its highest point
- A steadily decreasing upward acceleration from the moment the cannonball leaves the cannon barrel until it reaches its highest point
- o A constant upward acceleration
- A constant downward acceleration

Fg is only force

## 2. PhET Simulation

Drag the cannon downwards so it is at ground level, or 0 m (which represents the initial height of the object), then fire the pumpkin straight upward (at an angle of 90°) with an initial speed of 14 m/s. How long does it take for the pumpkin to hit the ground?

2.85 s

When the pumpkin is shot straight upward with an initial speed of 14 m/s, what is the maximum height above its initial location?

9.99 m

If the initial speed of the pumpkin is doubled, how does the maximum height change?

• The maximum height increases by a factor of two.

The maximum height increases by a factor of four.

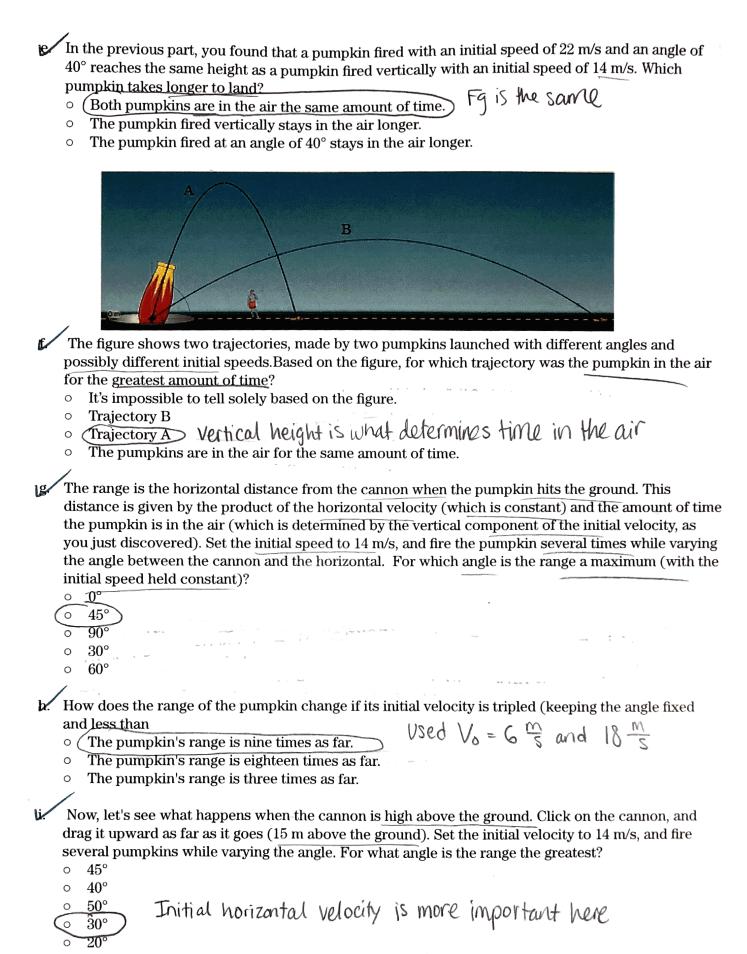
39.64 m

- The maximum height increases by a factor of 1.4 (square root of 2).
- Erase all the trajectories, and fire the pumpkin vertically again with an initial speed of 14 m/s. As you found earlier, the maximum height is 9.99 m. If the pumpkin isn't fired vertically, but at an angle less than 90°, it can reach the same maximum height if its initial speed is faster. Set the initial speed to 22 m/s, and find the angle such that the maximum height is roughly the same. Experiment by firing the pumpkin with many different angles. What is this angle?

○ 35° ○ 40° ○ 45°

Maximum height = 10.19 m

- o 50°
- o 55°



- So far in this tutorial, you have been launching a pumpkin. Let's see what happens to the trajectory if you launch something bigger and heavier, like a car. Compare the trajectory and range of the pumpkin to that of the car, using the same initial speed and angle (e.g., 45°). (Be sure that air resistance is still turned off.) Which statement is true?
  - The trajectories differ; the range of the car is shorter than that of the pumpkin.
  - The trajectories differ; the range of the car is longer than that of the pumpkin.
  - The trajectories and thus the range of the car and the pumpkin are identical.

Trajectory with no air resistance doesn't depend or

In the previous part, you discovered that the trajectory of an object does not depend on the object's prize or mass. But if you have ever seen a parachutist or a feather falling, you know this isn't really true. That is because we have been neglecting air resistance, and we will now study its effects here. For the following parts, select the "Lab" mode of the simulation found at the bottom of the screen. Notice that you can adjust the mass and diameter of the object being launched. Turn on Air Resistance by checking the box. Fire a cannonball with an initial speed of 18 m/s and an angle of 45°. Compare the trajectory to the case without air resistance. How do the trajectories differ?

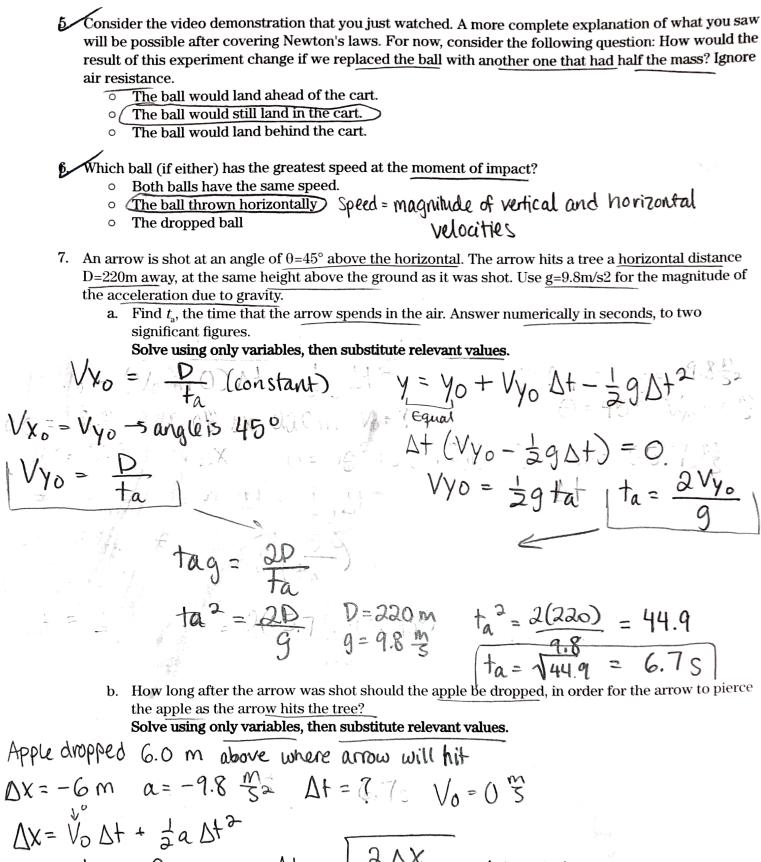
- (The trajectory with air resistance has a shorter range.)
- The trajectory with air resistance has a longer range.
- The trajectories are identical.

What happens to the trajectory of the cannonball when you increase the diameter while keeping the mass constant?

- Increasing the size makes the range of the trajectory decrease.
- Increasing the size makes the range of the trajectory increase.
- The size of the object doesn't affect the trajectory.
- You might think that it is never a good approximation to ignore air resistance. However, often it is. Fire the cannonball without air resistance, and then fire it with air resistance (same angle and initial speed). Then, adjust the mass of the cannonball (increase it and decrease it) and see what happens to the trajectory. Don't change the diameter. When does the range with air resistance approach the range without air resistance?
  - It never does. Regardless of the mass, the range with air resistance is always shorter than the range without.
  - The range with air resistance approaches the range without air resistance as the mass of the cannonball is decreased.
  - The range with air resistance approaches the range without air resistance as the mass of the cannonball is increased.
- B. The crew of a cargo plane wishes to drop a <u>crate of supplies</u> on a target below. To hit the target, when should the <u>crate?</u> Ignore air resistance.
  - When the plane is directly over the target
  - (Before the plane is directly over the target
  - After the plane has flown over the target

Which projectile spends more time in the air, the one fired from 30° or the one fired from 60°?

- · (The one fired from 60°) Greater vertical height
- The one fired from 30°
- They both spend the same amount of time in the air.



 $\Delta X = -6 \text{ m} \quad \alpha = -9.8 \frac{m}{52} \quad \Delta t = 7.7 \quad V_0 = 0 \frac{m}{5}$   $\Delta X = \frac{1}{2} \alpha \Delta t^2 \qquad \Delta t = \sqrt{\frac{2\Delta X}{g}} \quad \Delta t = 1.1 \text{ s}$   $\Delta Y = \frac{1}{2} \alpha \Delta t^2 \qquad \Delta t = \sqrt{\frac{2\Delta X}{g}} \quad \Delta t = 1.1 \text{ s}$   $\Delta Y = \frac{2\Delta X}{g} \qquad \text{Takes arrow } 6.7 \text{ seconds, so wait}$  6.7 - 1.1 = 5.6 seconds to drop apple

The archerfish is a type of fish well known for its ability to catch resting insects by spitting a jet of water at them. This spitting ability is enabled by the presence of a groove in the roof of the mouth of the archerfish. The groove forms a long, narrow tube when the fish places its tongue against it and propels drops of water along the tube by compressing its gill covers.

When an archerfish is hunting, its body shape allows it to swim very close to the water surface and look upward without creating a disturbance. The fish can then bring the tip of its mouth close to the surface and shoot the drops of water at the insects resting on overhead vegetation or floating on the water surface.

At what speed v should an archerfish spit the water to shoot down an insect floating on the water surface located at a distance 0.800 m from the fish? Assume that the fish is located very close to the surface of the pond and spits the water at an angle 60° above the water surface.

Solve using only variables, then substitute relevant values.

Solve using only variables, then substitute relevant values.

$$y = y_0 + (V_0 \sin \emptyset) \Delta + -\frac{1}{2}g\Delta + \frac{1}{2}g\Delta +$$

b. Now assume that the insect, instead of floating on the surface, is resting on a leaf above the water surface at a horizontal distance 0.600 m away from the fish. The archerfish successfully shoots down the resting insect by spitting water drops at the same angle 60° above the surface and with the same initial speed v as before. At what height h above the surface was the insect? Solve using only variables, then substitute relevant values.

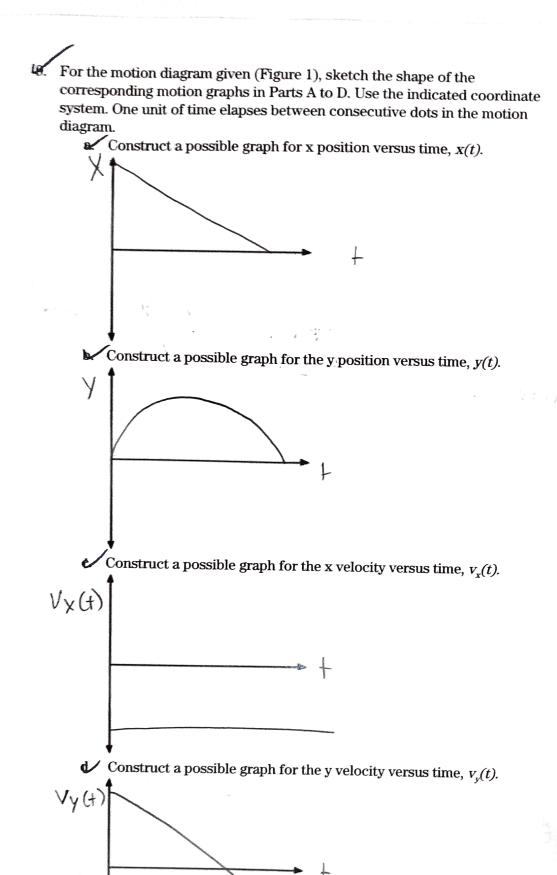
Solve using only variables, then substitute relevant values.

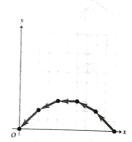
$$V_0 = 3.01 \frac{m}{3} \quad \text{Constant honizontal velocity}$$

$$V_X = V_0 \cos \theta = 3.01 \cos (60^\circ) = 1.5 \frac{m}{3}$$

$$V_X = \frac{\Delta x}{\Delta t} \quad 1.5 \frac{m}{3} = \frac{0.600 \text{ m}}{\Delta t} \quad \Delta t = 0.45$$

$$y = y_0 + (V_0 \sin \theta) \Delta t - \frac{1}{2} g \Delta t^2$$
  
 $y = [3.01 \sin (60)][0.399 s] - \frac{1}{2} (-9.8)[-0.399^2]$   
 $y = [1.039] - 0.779$   
 $y = 0.260 \text{ m}$ 

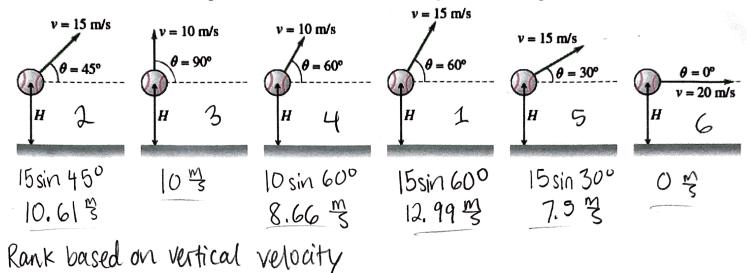




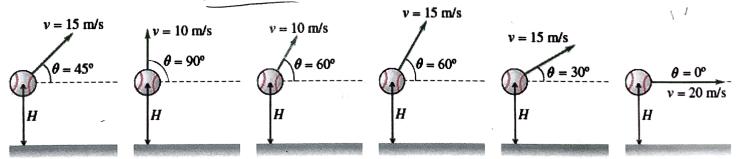
10.

Rank these throws based on the maximum height reached by the ball.

Rank from largest to smallest. To rank items as equivalent, overlap them.



Rank these throws based on the amount of time it takes the ball to hit the ground. Rank from largest to smallest. To rank items as equivalent, overlap them.



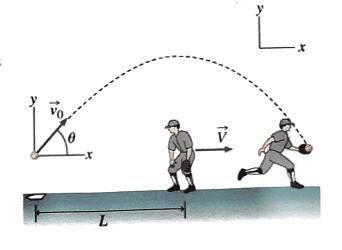
Vertical velocity determines time in the air Same ranking as above

11. (Figure 1) A softball is hit over a third baseman's head with some speed v0 at an angle  $\theta$  above the horizontal. Immediately after the ball is hit, the third baseman turns around and begins to run at a constant velocity V=7.00m/s. He catches the ball  $\underline{t=2.00s}$  later at the same height at which it left the bat. The third baseman was originally standing L=18.0m from the location at which the ball was hit.

Find  $v_0$ . Use g=9.81m/s<sup>2</sup> for the magnitude of the acceleration due to gravity.

Solve using only variables, then substitute

relevant values.



Third baseman 
$$V=7\%$$
  $X_0=18m \Delta t=2s$   
 $X_f=X_0+V\Delta t$   $X_f=18+7(2)=132m$   
 $X=L+Vt$   $Y=Y_0+(4\sin 4)\Delta t$ 

$$y=0 y_0=0$$

$$V_0 \bar{y} = \frac{1}{2}g\Delta t$$

$$V_0 = \sqrt{\frac{(L+V+)^2}{+}} + (\frac{1}{2}9\Delta +)^2 = \sqrt{16^2 + (-9.8)^2} = \sqrt{352.04}$$

$$V_0 = 18.8 \frac{m}{3}$$

Find the angle  $\theta$  in degrees.

Solve using only variables, then substitute relevant values.

$$V_y = V_0 \sin \theta$$

$$\Theta = \arcsin \left(\frac{V_V}{V_0}\right) = \arcsin \left(\frac{9.8}{18.8}\right)$$

$$\Theta = 31.5^{\circ}$$

12. A frog jumps at an angle 30° above the horizontal. The origin of the coordinate system is at the point where the frog leaves the ground. Assume the x-axis is directed horizontally in the direction of the frog's motion, and the y-axis is directed upward. Complete the table by putting cross and check marks in the cells. If a physical quantity in the first column that describes the motion of the frog corresponds to the description in the first row of what is happening to this quantitiy while the frog is moving, put a check mark into the cell, but otherwise put a cross mark. Consider the frog as a point-like object, and assume that the resistive force exerted by the air is negligible.

- X coordinate magnitude always increases (goes away from origin)	S Physical quantity	Remains constant	Is changing	Increases only	Decreases only	Increases, then decreases	Decreases, then increases
- Y coordinate increases (going up) then	x-coordinate magnitude	X		V	X	X	X
decreases (going down?	y-coordinate magnitude	X		X	X		X
Velocity always decreases (positive a		X	V	X		X	X
Slowing down, negative and speeding up- Magnitude of velocity decreases the		X		X	X	X	
increases (negative +speeding up -> magnitude			X	X	X	X	X
- Acceleration is uniform (Net force is	Magnitude of acceleration	V	X	X	X	X	$\left[\mathcal{X}\right]$
1010613	17)			,			

13. You can shoot an arrow straight up so that it reaches the top of a 31 -m-tall building. The arrow starts 1,45 m above the ground.

**a** How far will the arrow travel if you shoot it horizontally while pulling the bow in the same way? Neglect the air resistance. Vo = 24.07 4

Solve using only variables, then substitute relevant values.

Yo = 1.45 m 
$$a = -9.8 \frac{m}{s^2}$$
  $V_f^2 = V_0^2 + 2a\Delta x$   
Yf = 31 m  $V_f^2 = 0.55$   $V_0^2 = 579.18$ 

$$Y = Y_0 + (Vosin 0)\Delta t - \frac{1}{2}g\Delta t^2$$
  $\theta = 0$   $Y = 0$   $M_1$   $Y_0 = 1.45$   $M_2 = V_0 \cos \theta = 24.07 \cos \theta = 24.07$   $\Delta t^2 = 0.296$   $\Delta t = 0.544$   $\Delta t = 0.544$   $\Delta t = 0.544$   $\Delta t = 0.544$ 

Where do you need to put a target that is 1.45 m above the ground in order to hit it if you aim 30° above the horizontal while pulling the bow in the same way? Solve using only variables, then substitute relevant values

$$V_0 = 24.07 \stackrel{\text{M}}{>} Y_0 = 1.45 \text{ m} \quad y_f = 1.45 \text{ m} \quad \theta = 30^\circ$$

$$Y = Y_0 + (V_0 \sin \theta) \Delta t - \frac{1}{2}g \Delta t^2 \qquad V_X = \frac{\Delta x}{\Delta t}$$

$$\Delta t = \frac{\Delta V_0 \sin \theta}{2} = \frac{1}{2}g \Delta t$$

$$\Delta t = \frac{\Delta V_0 \sin \theta}{2} = \frac{1}{2}g \Delta t$$

$$\Delta t = \frac{\Delta V_0 \sin \theta}{2} = \frac{1}{2}g \Delta t$$

$$\Delta t = \frac{\Delta V_0 \sin \theta}{2} = \frac{1}{2}g \Delta t$$
Place the tan

$$V_X = V_0 \cos \theta = 24.07 \cos 30^\circ = 20.84 \frac{S}{S}$$

$$V_X = \frac{\Delta X}{\Delta Y} = 20.84 = \frac{\Delta X}{2.46}$$

$$D_1 = \frac{\Delta X}{2.46}$$
Place the target 51 m away

Math to 11